

A3 Index to mathematical notation and symbols

Matrices and vectors

A = matrix containing elements $a_{ij} = -\frac{1}{2} d_{ij}^2$

B = matrix of variables ($N \times s$) that are linear combinations of normalised **X** variables having maximum correlation with CAP axes

C = matrix of CAP axes ($N \times s$), standardised by the square root of their respective eigenvalues

D = matrix containing elements d_{ij} corresponding to distances or dissimilarities

G = Gower's centred matrix, consisting of elements $g_{ij} = a_{ij} - \bar{a}_{i\bullet} - \bar{a}_{\bullet j} + \bar{a}_{\bullet\bullet}$

H = 'hat' matrix = $\mathbf{X}(\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'$, used as a projection matrix for regression models

I = identity matrix, with 1's along the diagonal and 0's elsewhere

Q = matrix of PCO axes, standardised by the square root of their respective eigenvalues

\mathbf{Q}^0 = matrix of PCO axes, orthonormalised to SSCP = **I** ('sphericised')
U = matrix whose columns contain the left singular vectors from a singular value decomposition (SVD) of a matrix (e.g., $\mathbf{X} = \mathbf{U}\mathbf{W}\mathbf{V}'$); if **X** is ($N \times q$) and $q < N$, then **U** is ($N \times q$)

V = matrix whose columns contain the right singular vectors from a singular value decomposition (SVD) of a matrix (e.g., $\mathbf{X} = \mathbf{U}\mathbf{W}\mathbf{V}'$); if **X** is ($N \times q$) and $q < N$, then **V** is ($q \times N$)

W = diagonal matrix of eigenvalues from a singular value decomposition (SVD) of a matrix (e.g., $\mathbf{X} = \mathbf{U}\mathbf{W}\mathbf{V}'$); if **X** is ($N \times q$) and $q < N$, then **W** is ($q \times q$)

X = matrix of predictor variables ($N \times q$) (often a set of environmental variables)

\mathbf{X}^0 = matrix of **X** variables, orthonormalised to SSCP = **I** ('sphericised')

Y = matrix of response variables ($N \times p$) (often a set of species variables)

\mathbf{Y}^0 = matrix of **Y** variables, orthonormalised to SSCP = **I** ('sphericised')

$\hat{\mathbf{Y}} = \mathbf{H}\mathbf{Y}$ = matrix of fitted values ($N \times p$)

\mathbf{y}_{ij} = vector of p response variables for the j th observation in the i th group

$\bar{\mathbf{y}} =$ the centroid vector of p response variables for group i

Z = matrix of dbRDA canonical axes ($N \times s$)

Letters

a, b, c , etc... = number of levels of factor A, B, C, etc... in an ANOVA experimental design

AIC = multivariate analogue to Akaike's information criterion

AIC_c = multivariate analogue to the small-sample-size corrected version of AIC

B_l = the l th variable in the space of normalised **X** variables that has maximum correlation with the l th coordinate axis (C_l) from a CAP analysis

BIC = multivariate analogue to Schwarz's 'Bayesian information criterion'
 C_{il} = the l th coordinate axis scores from a CAP analysis
 d_{ij} = distance or dissimilarity between sample i and sample j df = degrees of freedom
 F = pseudo- F statistic for testing hypotheses in PERMANOVA or DISTLM
 i = index used for samples (i.e., $i = 1, \dots, N$) or index used for groups ($i = 1, \dots, a$)
 j = second index used for samples (i.e., $j = 1, \dots, N$) or index used for replicates within a group ($j = 1, \dots, n$)
 k = index used for variables (i.e., $k = 1, \dots, p$ or else $k = 1, \dots, q$)
 l = index used for canonical axes or eigenvalues for either dbRDA or CAP (i.e., $l = 1, \dots, s$) or either the abbreviation for 'log-likelihood' or the 'length' of a vector (depending on context).
 m = number of PCO axes chosen as a subset for analysis by CAP MC = Monte Carlo
 MS = mean square
 N = total number of samples
 n = number of samples (replicates) within a group or cell in an experimental design
 P = P -value associated with the test of a null hypothesis p = number of multivariate response variables in matrix \mathbf{Y} q = total number of predictor variables in matrix \mathbf{X}
 r = Pearson correlation coefficient
 R = the ANOSIM R statistic (see Clarke 1993)
 R^2 = proportion of explained variation from a model
 s = number of canonical eigenvalues and associated canonical axes obtained from either a dbRDA or a CAP analysis SS = sum of squares
 $SSCP$ = sum of squares and cross products
 SVD = singular value decomposition
 t = pseudo- t statistic = $\sqrt{\text{pseudo-}F}$
 tr = 'trace' of a matrix = the sum of the diagonal elements
 X_k = the k th predictor variable
 Y_k = the k th response variable
 z_{ij} = distance to group centroid for the j th replicate within the i th group.

Greek symbols and matrices

α = significance level chosen for a test (usually $\alpha = 0.05$).
 Δ_l^2 = the l th eigenvalue from a CAP analysis, a squared canonical correlation
 Δ = diagonal matrix containing the square roots of the eigenvalues from a CAP analysis (a capital delta)
 γ_l^2 = the l th eigenvalue from a dbRDA analysis, a portion of the explained (regression) sum of squares from a dbRDA model.
 Γ = diagonal matrix containing the square roots of the eigenvalues from a dbRDA analysis (a capital gamma)
 λ_i = the i th eigenvalue from a PCO analysis
 Λ = diagonal matrix of eigenvalues from a PCO analysis (a capital lambda)
 ν = number of parameters in a particular model during model selection
 ρ = Spearman rank correlation (rho)
 \sum = sum over the relevant index

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